

Multi-view stereo analysis reveals anisotropy of prestrain, deformation, and growth in living skin

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Abstract Skin expansion delivers newly grown skin that maintains histological and mechanical features of the original tissue. Although it is the gold standard for cutaneous defect correction today, the underlying mechanisms remain poorly understood. Here we present a novel technique to quantify anisotropic prestrain, deformation, and growth in a porcine skin expansion model. Building on our recently proposed method, we combine two novel technologies, multi-view stereo and isogeometric analysis, to characterize skin kinematics: Upon explantation, a unit square retracts *ex vivo* to a square of average dimensions of 0.83×0.83 . Upon expansion, the unit square deforms *in vivo* into a rectangle of average dimensions of 1.40×1.34 . Deformations are larger parallel than perpendicular to the dorsal midline suggesting that skin responds anisotropically with smaller deformations along the skin tension lines. Upon expansion, the patch grows *in vivo* by 1.62×1.40 with respect to the explanted, unexpanded state. Growth is larger parallel than perpendic-

ular to the midline, suggesting that elevated stretch activates mechanotransduction pathways to stimulate tissue growth. The proposed method provides a powerful tool to characterize the kinematics of living skin. Our results shed light on the mechanobiology of skin and help us to better understand and optimize clinically relevant procedures in plastic and reconstructive surgery.

Keywords Multi-view stereo · Isogeometric analysis · Anisotropy · Prestrain · Growth · Skin

1 Introduction

Skin expansion is a common technique in plastic and reconstructive surgery (Neumann 1957). It is based on the evidence that skin grows and remodels to achieve mechanical homeostasis (De Filippo and Atala 2002; Silver et al. 2003). During the procedure, an expander is placed below the skin and inflated periodically to chronically overstretch the tissue beyond its physiological limit (Pamplona et al. 2014; Zöllner et al. 2012). Skin grows *in situ* producing local flaps that can be used to correct large defects such as giant congenital nevi, burn injuries, and regions of tumor removal (Gosain et al. 2001; LoGiudice and Gosain 2003; Marcus et al. 1990). Figure 1 illustrates the use of skin expansion to correct a cutaneous defect in a one-year-old boy with a giant congenital nevus (Zöllner et al. 2013). To grow extra skin for defect repair, two tissue expanders are implanted and gradually filled with saline solution, left. Expander inflation creates mechanical overstretch and triggers controlled skin growth, middle. After several weeks, the expanders are removed, the nevus is excised, and the defect area is covered with the newly grown skin, right (Buganza Tepole et al. 2014). One preeminent advantage of this technique is the production of skin

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Fig. 1 Skin expansion is routinely performed in reconstructive surgery to correct large cutaneous defects. To grow extra skin for defect repair, tissue expanders are implanted underneath the skin, *left*. The expanders are gradually filled with saline solution to apply mechanical overstretch and trigger controlled skin growth, *middle*. Several weeks postimplantation, the expanders are removed, the defect is excised, and the defect area is covered by the newly grown skin, *right*

with the same hair, mechanical properties, color and texture of the surrounding tissue, making it ideal from an aesthetic point of view (Rivera et al. 2005). At the same time, tissue expansion remains challenging, several open questions prevail, and surgeons have to rely on their own decade-long experience to successfully plan and execute this technique (Bhandari 2009).

In response to the indisputable importance of mechanical factors during the skin expansion process (Pietramaggiore et al. 2007), we have proposed a mathematical model to capture the relationship between overstretch and skin adaptation using the theory of finite growth within a continuum mechanics framework (Buganza Tepole et al. 2012). We have successfully applied our model to different expander geometries as well as different patient specific scenarios, and we have shown good qualitative comparison with the clinical observations (Buganza Tepole et al. 2011; Zöllner et al. 2012). Computational models are being steadily integrated into medical applications and hold the promise of enhancing medical device design and improving treatments efficacy in reconstructive surgery (Buganza Tepole et al. 2014). Measuring and predicting prestrain, deformation, and growth during a routine skin expansion procedure is practically impossible, and the usefulness of a computational approach is unquestionable (Pamplona and Carvalho 2012). However, despite the increasing acceptance of computational tools, their integration into clinically relevant scenarios is slow due to the lack of experimental data to calibrate and validate the models.

Here we establish a chronic porcine model to quantify skin kinematics during tissue expansion. This work builds on our recently proposed methodology to characterize prestrain, deformation, and growth (Buganza Tepole et al. 2014). Our experimental setup uses two novel technologies that allow us to obtain the desired data without imposing constraints on a regular expansion procedure: We employ multi-view stereo techniques to reconstruct the three-dimensional geometry out of photographs and adopt isogeometric analysis tools

to describe the kinematics of thin membranes. We decompose the total deformation of tissue expansion using the concept of incompatible configurations. The continuum interpolation of the displacement field allows us to quantify regional variations of prestrain, deformation, and growth.

Multi-view stereo (MVS) is the extraction of three-dimensional geometries out of photographs. Originally motivated by the need of creating volumetric representations from medical images, this field of computer vision has seen growing research interest in the past decade (Hiep et al. 2009; Seitz et al. 2006). In a very simplistic manner, MVS can be understood by considering first binocular stereo. Animals generate depth information from two images since the brain knows the calibration parameters of one eye with respect to the other. In MVS algorithms, such parameters are unknown, however, by having many pairs of images from a single scene, we can determine the calibration values based on feature matching (Cyganek and Siebert 2009). The accuracy of MVS, with errors as low as 2%, together with its low cost and ease of use, rivals once believed unbeatable reconstruction techniques such as laser scanning (Furukawa and Ponce 2010). In the field of experimental biomechanics, common reconstruction techniques employ restrictive experimental setups and specialized equipment to track material points (Mahmud et al. 2010; Tonge et al. 2013). The fact that we can readily appreciate the deformations of skin with our naked eye naturally suggests the possibility of capturing its shape by tracking a few interpolatory points with MVS techniques.

B-splines are used commonly as basis functions for smooth interpolation of curves and surfaces in the CAD (Computer Aided Design) industry (Piegl and Tiller 1987). Mechanical analysis relies heavily on the finite element technologies based on discretizing the spatial domain by meshing it into several small pieces (Hughes 1987). Recently, an effort to bridge the gap between design and analysis has brought forth isogeometric analysis (IGA) (Hughes et al. 2005). The main idea behind IGA is to employ the same basis functions that lie beneath the CAD technology to solve partial differential equations in the exact geometric representation. IGA has received significant attention in recent years and has shown tremendous potential for thin shell analysis (Kiendl et al. 2009). B-spline basis functions offer an advantageous building block for smooth parametric representation of surfaces with high continuity and good approximation over relatively coarse meshes (Buganza Tepole et al. 2014).

During skin expansion, tracking a small set of points becomes practical with MVS algorithms. Then, from the coordinates of a few material points, B-spline tensor product patches with a prescribed parametrization can smoothly interpolate deformations using the IGA concept. Using simple finite element meshes to parametrize the deformation would yield strain fields with poor spatial resolution and would require additional subdivision steps (Göktepe et al. 2010).

Skin is a thin biological membrane that constitutes our interface with the outside world displaying noteworthy mechanical properties under large strains (Flynn et al. 2011). Like all biological systems, it actively adapts to its mechanical environment by growth, remodeling, and morphogenesis (Taber 1995). When skin is mechanically loaded, the observable changes in the geometrical configuration over time become a combination of reversible and irreversible contributions (Ambrosi et al. 2014). The deformation gradient extracted from the IGA membrane description is the key object that links mechanical cues to the final amount of skin growth. For soft tissues, growth can be expressed kinematically through the multiplicative decomposition of the deformation gradient into elastic and growth components (Kuhl 2014). For skin as a thin membrane, we assume that growth takes place exclusively in the plane, and the growth tensor is symmetric and orthotropic (Zöllner et al. 2013).

2 Methods

2.1 Animal model

Porcine models are a natural choice for tissue expansion (Bartell and Mustoe 1989). Experiments in porcine models have improved our understanding of the histological and biomechanical changes of skin upon hyper-stretch (Johnson et al. 1988). The main reason to choose a porcine expansion model is the similarity between the anatomical and mechanical characteristics of human and young porcine integument (Meyer et al. 1981, 1982; Montagna and Yun 1964). From a clinical point of view, tissue expansion in the pig is similar to tissue expansion in humans, with similar criteria for expander selection, filling volume, and inflation timing (Bartell and Mustoe 1989).

2.1.1 Surgical procedure

We perform skin expansion on a month-old Yucatan pig (Sinclair Biolabs, Columbus, MO, USA) (Buganza Tepole et al. 2014). The pig acclimated to the laboratory facilities at the Robert H. Lurie Children's Hospital of Chicago according to approved protocols. Following the arrangement in Fig. 2, we tattoo four 10 cm × 10 cm grids on the back of the pig, symmetrically with respect to the midline. We parameterize each grid discretely with coordinates in the interval [0, 10] along the directions G_1 and G_2 . We implant two expanders of 4 cm × 6 cm with filling volumes of 120 cc as shown in Fig. 3 (PMT Corporation, Chanhassen, MN), one in the anterior-right grid Q, and one in the posterior-left R. Grids P and S serve as controls. After inserting the expanders, we wait 14 days to allow the wounds to heal until we remove the sutures.

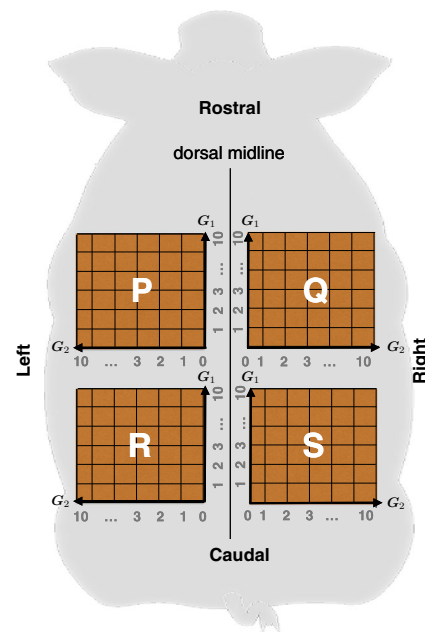


Fig. 2 Nomenclature for the tattooed grids on the porcine model. We label the grids as P anterior-left, Q anterior-right, R posterior-left, and S posterior-right. Symmetry with respect to the midline ensures expanded and control grids. Coordinates on the grid parametrize each zone along the directions G_1 , parallel to the dorsal midline, and G_2 , perpendicular to the dorsal midline along the skin tension lines

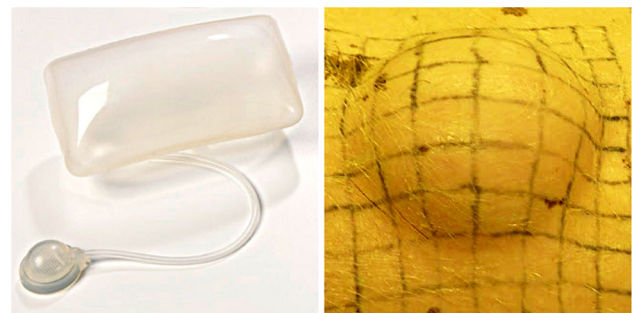


Fig. 3 Skin expansion in a chronic porcine model. The rectangular tissue expander, *left*, is implanted subcutaneously underneath a tattooed 10 cm × 10 cm grid and gradually inflated over a period of 5 weeks. Skin expansion creates mechanical overstretch and triggers controlled skin growth, *right*

2.1.2 Skin expansion

Expansion begins after the initial sutures heal. On day $t = 0$, we begin the expansion by injecting 25 cc of saline solution into the anterior expander Q and 50 cc into the posterior expander R. We repeat this protocol weekly at days $t = 8, 15, 22,$ and 29 . On day $t = 35$, we complete the expansion with a final injection of 15 and 30 cc into the anterior Q and posterior R expanders. Each week, we acquire the deformation by taking 15 photographs from different angles, both before and after expansion.

2.1.3 Tissue harvest and euthanasia

On day $t = 38$, we anesthetize the animal and acquire the last set of in vivo photographs of the tattooed grids. We then euthanize the animal by using intravenous overdose of pentobarbital (90 mg/kg) and excise the four grids. We photograph the excised samples ex vivo for further reconstruction and analysis.

2.2 Multi-view stereo

At the end of the experiment, we have collected seven sets of photographs, preexpansion and postexpansion, from 15 different angles for each grid (Buganza Tepole et al. 2014). Figure 4, middle, illustrates this setting. MVS algorithms match common points in pairs of photographs to calculate the camera position and extract the coordinates of these points in the three-dimensional Euclidean space \mathbb{R}^3 . The details of MVS algorithms escape the focus of the present publication; we refer the interested reader to the literature for further details (Cyanek and Siebert 2009). We adopt an online service for the geometric reconstruction of our experimental setup (Autodesk 2014). Figure 4, top, shows four different views of a particular time point of interest, while Fig. 4, bottom, illustrates the resulting surface reconstruction approximated with a triangular mesh.

To quantify the accuracy of the reconstruction, we include a ruler in the photograph and we fit a cubic spline to the points to the 1 cm marks of the ruler. We calculate the length l_i between every pair of points along the spline and obtain the average length \bar{l} . We defined the relative reconstruction error e as

$$e = \frac{\sum e_i}{n} \quad \text{with} \quad e_i = \frac{l_i - \bar{l}}{\bar{l}}, \quad (1)$$

where n is the number of spline sections and \bar{l} is the scaling factor with respect to the physical world where $\bar{l} = 1$ cm. Figure 2 illustrates each grid with 121 material points parametrized by a tensor product space of coordinates along directions \mathbf{G}_1 , parallel to the dorsal midline, and \mathbf{G}_2 , perpendicular to the dorsal midline along the skin tension lines. For example, the points $\mathbf{P}_{ab}^t \in \mathbb{R}^3$ from the MVS reconstruction specify the grid \mathbf{P} at time t , with a, b the integers in the interval $[0, 10]$.

2.3 B-Spline-based isogeometric analysis

2.3.1 B-spline curves

A B-spline curve is a piecewise polynomial function that maps a segment of a line to the three-dimensional Euclidean space $\boldsymbol{\gamma} : \xi \in \mathbb{R} \rightarrow \mathbb{R}^3$. The representation of B-spline curve

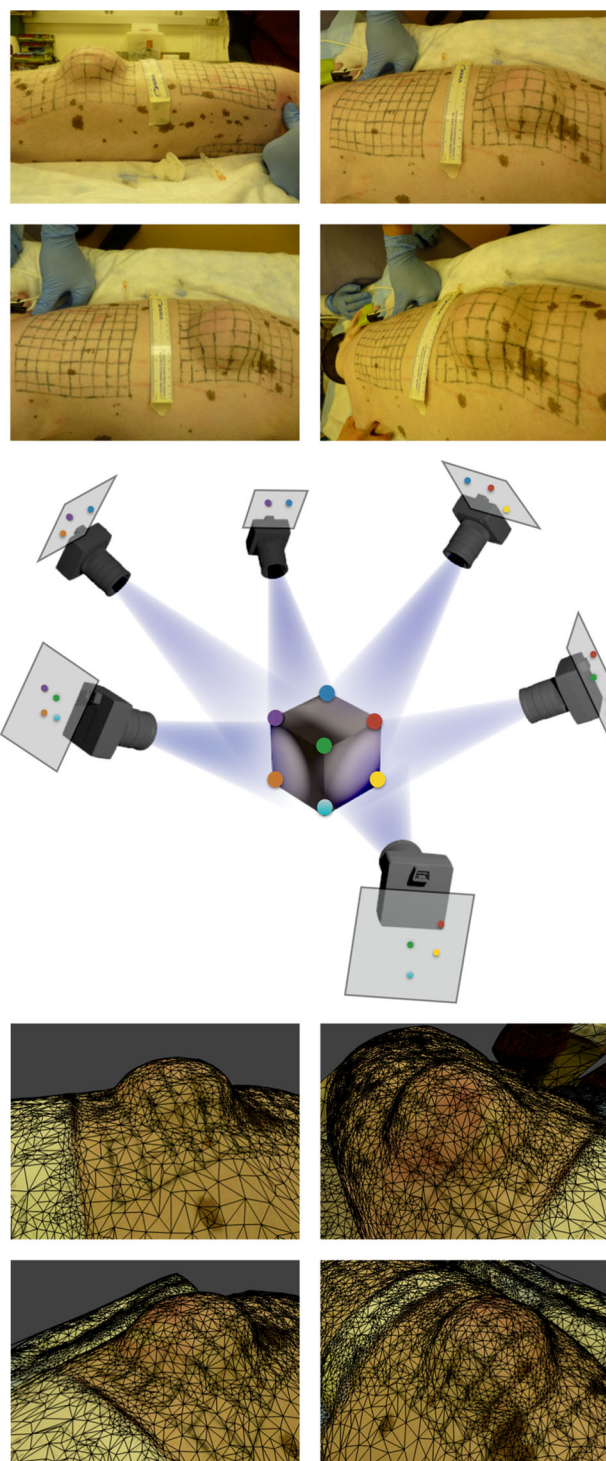


Fig. 4 Multi-view stereo (MVS) reconstruction. The *top* shows four photographs of the experimental setup. As illustrated in the *middle*, the MVS algorithm finds common features between pairs of photographs to find the camera calibration parameters. The *bottom* depicts four different views of the reconstructed, triangulated surface

of degree p requires a knot vector $\boldsymbol{\xi}$ and a set of control points $\mathbf{P}_i \in \mathbb{R}^3$. The knot vector consists of non-decreasing numbers $\boldsymbol{\xi} = [\xi_0, \xi_1, \dots, \xi_n]$. The number of control points

is $m = n - p - 1$. The first and last values of the knot vector ξ_0 and ξ_n are repeated $p + 1$ times. We define basis functions recursively. The zeroth order basis functions are

$$N_{i,0} = \begin{cases} 1 & \xi_i \leq \xi < \xi_{i+1} \\ 0 & \text{otherwise.} \end{cases} \quad (2)$$

Higher-order functions of degree $p \geq 1$ follow from the recursive definition,

$$N_{i,p} = \frac{\xi - \xi_i}{\xi_{i+p} - \xi_i} N_{i,p-1}(\xi) + \frac{\xi_{i+p+1} - \xi}{\xi_{i+p+1} - \xi_{i+1}} N_{i+1,p-1}(\xi). \quad (3)$$

The B-spline curve γ is the sum of the basis functions and control points,

$$\gamma = \sum_{i=0}^m N_{i,p}(\xi) P_i. \quad (4)$$

2.3.2 B-spline surfaces

There are several alternatives to create surfaces based on B-spline basis functions. We employ tensor product surfaces, which are constructed from a tensor product of two B-spline curves. A B-spline surface is a map from the parametric two-dimensional space to the Euclidean three-dimensional space $\mathcal{S} : \xi = [\xi, \eta] \in \mathbb{R} \times \mathbb{R} \rightarrow \mathbb{R}^3$. This implies that we require two knot vectors Ξ and Ω that define two sets of basis functions $N_{i,p}$ and $Q_{j,q}$. The B-spline surface is then defined with the control net $P_{i,j} \in \mathbb{R}^3$

$$S = \sum_{i=0}^m \sum_{j=0}^r N_{i,p}(\xi) Q_{j,q}(\eta) P_{i,j} \quad (5)$$

2.3.3 B-spline isogeometric analysis of skin expansion

Here we explain the analysis for region P, but it similarly applies for the other three regions Q, R, and S. We begin with the 121 points P_{ab}^t for time t . We fit a bi-cubic B-spline surface patch $\mathcal{S}^t(\xi, \eta)$ with the following parametrization: We choose the knot vectors to be $\xi = \eta = [0, 0, 0, 0, 2, 3, \dots, 9, 10, 10, 10, 10]$, and we interpolate such that $P_{ab}^t = \mathcal{S}^t(\hat{\xi}_a, \hat{\eta}_b) \forall t$, with $\hat{\xi}_a = a, \hat{\eta}_b = b$ constant for all interpolations. As a result, the parametrization remains the same for any time point.

Any given pair of time points $t = t_1, t_2$ defines a pair of surfaces $\mathcal{S} = \mathcal{S}^{t_1}, \mathcal{S}^{t_2}$. We choose t_1 as the reference and t_2 as the deformed configuration of the mid-surface of the membrane under study. Figure 5-left shows the reference surface, \mathcal{S}^{t_1} , embedded from the parametric plane $\xi = [\xi, \eta] = \mathbb{R} \times \mathbb{R}$ into the three-dimensional Euclidean space. Figure 5-right shows the deformed surface, \mathcal{S}^{t_2} , also embedded from ξ . As a consequence of using the same parametric domain for

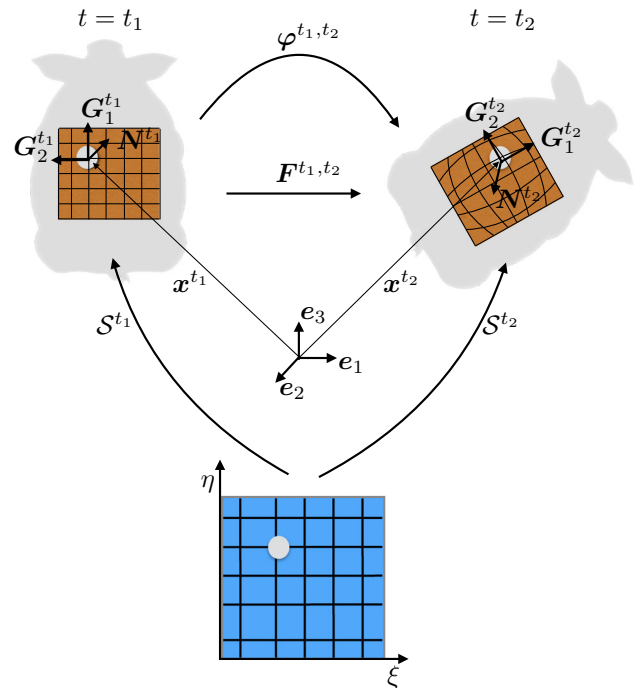


Fig. 5 Kinematics. Any pair of time points t_1, t_2 defines a pair of surface embeddings $\mathcal{S}^{t_1}, \mathcal{S}^{t_2}$ from the same parametric domain ξ into the three-dimensional space \mathbb{R}^3 . At every point x^i , the covariant vectors G_1^i, G_2^i span the tangent space of the surface, and together with the normal $N = G_3^i$ they are a basis for \mathbb{R}^3 . The same is true for x^{t_2} . The deformation map between the two configuration is φ^{t_1,t_2} , and its spatial gradient is F^{t_1,t_2}

both surfaces, points x^{t_1}, x^{t_2} follow from summation over the same basis functions R_{ab} ,

$$\begin{aligned} x^{t_1} &= \mathcal{S}^{t_1}(\xi) = \sum_{a,b=0}^{10} R_{ab}(\xi) P_{ab}^{t_1} \\ x^{t_2} &= \mathcal{S}^{t_2}(\xi) = \sum_{a,b=0}^{10} R_{ab}(\xi) P_{ab}^{t_2}. \end{aligned} \quad (6)$$

Figure 5 depicts the deformation map φ^{t_1,t_2} , which establishes the relationship between the reference and deformed membranes. The deformation map, $\varphi^{t_1,t_2}(\xi) : \mathcal{S}^{t_1} \rightarrow \mathcal{S}^{t_2}$, takes a material point from the reference surface, \mathcal{S}^{t_1} , to the position of that point on the deformed surface \mathcal{S}^{t_2} (Buganza Tepole et al. 2014). In Kirchhoff–Love kinematics, the normal to the reference mid-surface remains normal and there is no deformation across the thickness as the membrane deforms (Buganza Tepole et al. 2014). The material points of the deformed membrane can be located by a displacement vector u^{t_1,t_2} of the mid-surface alone,

$$x^{t_2} = \varphi^{t_1,t_2}(x^{t_1}) = \mathcal{S}^{t_2}(\xi) + u^{t_1,t_2}(\xi), \quad (7)$$

or, by incorporating the B-spline surface definition,

$$\mathbf{x}^{t_2} = \sum_{a,b=0}^{10} R_{ab}(\xi)(\mathbf{P}_{ab}^{t_1} + \mathbf{u}_{ab}^{t_1,t_2}). \tag{8}$$

Since our geometric description is based on curvilinear coordinates, the tangent space at the point \mathbf{x}^{t_1} is spanned locally by the covariant basis vectors,

$$\mathbf{G}_1^{t_1} = \sum_{a,b=0}^{10} R_{ab,\xi} \mathbf{P}_{ab}^{t_1} \tag{9}$$

$$\mathbf{G}_2^{t_1} = \sum_{a,b=0}^{10} R_{ab,\eta} \mathbf{P}_{ab}^{t_1},$$

where a comma denotes the partial differentiation. This implies that $\mathbf{G}_1^{t_1}$ are the tangent vectors to the coordinate lines aligned with the longitudinal axis of the pig, while $\mathbf{G}_2^{t_1}$ are the tangent vectors to the coordinate lines in the transverse direction illustrated in Figs. 2, 5. We extend the covariant basis vectors with the normal,

$$\mathbf{G}_3^{t_1} = N^{t_1} = \frac{\mathbf{G}_1^{t_1} \times \mathbf{G}_2^{t_1}}{\|\mathbf{G}_1^{t_1} \times \mathbf{G}_2^{t_1}\|}. \tag{10}$$

The triad $\mathbf{G}_i^{t_1}, i = 1, 2, 3$ spans the three-dimensional space \mathbb{R}^3 locally, at every point \mathbf{x}^{t_1} as shown in Fig. 5. The dual basis is composed of contravariant vectors $\mathbf{G}_i^{t_1}$ that satisfy $\mathbf{G}_i^{t_1} \cdot \mathbf{G}_j^{t_1} = \delta_j^i$, where δ_j^i denotes the Kronecker delta. The deformed covariant basis vectors follow from the partial differentiation of the deformed surface with respect to the parametric coordinates,

$$\mathbf{G}_1^{t_2} = \mathbf{G}_1^{t_1} + \sum_{a,b=0}^{10} R_{ab,\xi} \mathbf{u}_{ab}^{t_1,t_2} \tag{11}$$

$$\mathbf{G}_2^{t_2} = \mathbf{G}_2^{t_1} + \sum_{a,b=0}^{10} R_{ab,\eta} \mathbf{u}_{ab}^{t_1,t_2},$$

and we extend the set of these covariant basis with the deformed normal $\mathbf{G}_3^{t_2} = N^{t_2}$ such that $\mathbf{G}_i^{t_2}$ spans the three-dimensional space \mathbb{R}^3 at points \mathbf{x}^{t_2} . The dual basis of the deformed surface satisfies $\mathbf{G}_i^{t_2} \cdot \mathbf{G}_j^{t_2} = \delta_j^i$. The deformation gradient $\mathbf{F}^{t_1,t_2} = \partial \boldsymbol{\varphi}^{t_1,t_2} / \partial \mathbf{x}^{t_1}$ is the key kinematic object, it encapsulates the local deformation between the reference and deformed surfaces, \mathcal{S}^{t_1} and \mathcal{S}^{t_2} . Using the chain rule, we map the covariant base vectors of the reference configuration, $\mathbf{G}_i^{t_1}$, onto the covariant bases vectors of the deformed configuration, $\mathbf{G}_i^{t_2}$, as

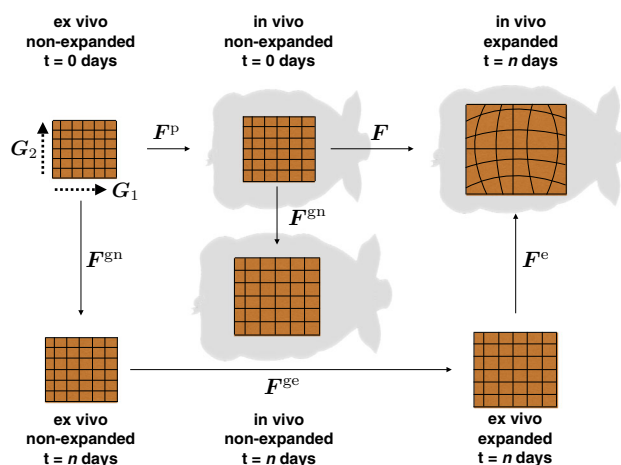


Fig. 6 Distinct configurations of the skin patch. In vivo, skin is subjected to prestrain, \mathbf{F}^P . Expansion induces deformation, \mathbf{F} . Excising the expanded patch releases the reversible, elastic deformation, \mathbf{F}^e . Skin growth, \mathbf{F}^g , consists of natural growth, \mathbf{F}^{gn} , and expansion-induced growth, \mathbf{F}^{ge}

$$\mathbf{G}_i^{t_2} = \frac{\partial \boldsymbol{\varphi}^{t_1,t_2}}{\partial \mathbf{x}^{t_1}} \frac{\partial \mathbf{x}^{t_1}}{\partial \xi^i} = \mathbf{F}^{t_1,t_2} \mathbf{G}_i^{t_1}. \tag{12}$$

The deformation gradient follows from the summation of the dyadic product of the covariant deformed and contravariant reference basis vectors,

$$\mathbf{F}^{t_1,t_2} = \mathbf{G}_i^{t_2} \otimes \mathbf{G}_i^{t_1}. \tag{13}$$

2.4 Kinematic analysis of skin expansion

Figure 6 displays all configurations of interest. At the beginning of expansion at day $t = 0$, skin in vivo is not stretch free (Menzel 2005): The deformation gradient with respect to the ex vivo state, denoted as \mathbf{F}^P , characterizes the prestrain state (Amini et al. 2012; Flynn et al. 2011). From the deformation gradient, we calculate the right Cauchy–Green deformation tensor \mathbf{C}^P . We are interested in three measures of stretch, the total area change,

$$\partial^P = \det(\mathbf{F}^P) \quad \text{with} \quad \mathbf{C}^P = \mathbf{F}^{P^t} \cdot \mathbf{F}^P, \tag{14}$$

and the two stretches in the covariant directions,

$$\lambda_1^P = \sqrt{\mathbf{G}_1 \cdot \mathbf{C}^P \cdot \mathbf{G}_1} \quad \text{and} \quad \lambda_2^P = \sqrt{\mathbf{G}_2 \cdot \mathbf{C}^P \cdot \mathbf{G}_2}, \tag{15}$$

parallel to the dorsal midline and perpendicular to the dorsal midline along the skin tension lines.

Figure 6 illustrates the deformation \mathbf{F} at day $t = n$ with respect to the in vivo state. The total deformation, $\mathbf{F} \cdot \mathbf{F}^P$, is not fully elastic. Growth can be captured kinematically by splitting the deformation gradient into elastic and growth contributions, $\mathbf{F}^e \cdot \mathbf{F}^g$. Figure 6 portrays the map between the ex vivo and the in vivo patch at day $t = n$, denoted as \mathbf{F}^e , which stores the elastic part. The growth part, \mathbf{F}^g , can be further decomposed into growth occurring naturally, \mathbf{F}^{gn} ,

and growth attributed exclusively to the expansion process F^{ge} ,

$$F \cdot F^P = F^e \cdot F^{ge} \cdot F^{gn} \tag{16}$$

This approach implies that only the elastic deformation, $F^e = F \cdot F^P \cdot F^{gn-1} \cdot F^{en-1}$, generates stress (Rausch et al. 2013). We assume that skin grows exclusively in the plane, while its thickness remains constant (Zöllner et al. 2012). We allow the in-plane area growth to be anisotropic with preferred directions G_1 and G_2 parallel and perpendicular to the midline, such that the growth tensor takes the following format (Göktepe et al. 2010),

$$F^g = \lambda_1^g G_1 \otimes G_1 + \lambda_2^g G_2 \otimes G_2 + N \otimes N. \tag{17}$$

This particular format allows us to multiplicatively correlate area changes associated with the total deformation ϑ , pre-strain ϑ^P , elastic deformation ϑ^e , expander-induced growth ϑ^{ge} , and natural growth ϑ^{gn} ,

$$\vartheta \vartheta^P = \vartheta^e \vartheta^{ge} \vartheta^{gn}. \tag{18}$$

The total area growth is simply the product of the stretches parallel and perpendicular to the midline, $\vartheta^g = \det(F^g) = \lambda_1^g \cdot \lambda_2^g$, where the anisotropic growth stretches $\lambda_1^g = \lambda_1^{gn} \lambda_1^{ge}$ and $\lambda_2^g = \lambda_2^{gn} \lambda_2^{ge}$ admit the split into natural and expander-induced contributions.

3 Results

We apply our mathematical analysis to the posterior region R and S. The anterior expansion P and Q failed due to port leakage. The entire expansion process spanned a period of $t = 37$ days. At the end of the procedure, the expander underneath the left-posterior grid R was filled to 280cc and the unexpanded right-posterior grid S served as control. Figure 7 shows the different configurations of the skin patches with the summary of our analysis. We are interested in quantifying three measures of local deformation: pre-strain, deformation, and growth. We have previously quantified isotropic area changes (Buganza Tepole et al. 2014), which we include here to complement our current orthotropic characterization.

3.1 Prestrain

Tissues in vivo are not stress free (Rausch and Kuhl 2013). Upon explantation, the flap of skin retracts revealing that skin in vivo is under some amount of deformation. Our experimental setup lets us use the unexpanded control patch to quantify the amount of prestrain. We create two three-dimensional models from the S patch at $t = 37$ days, once before the

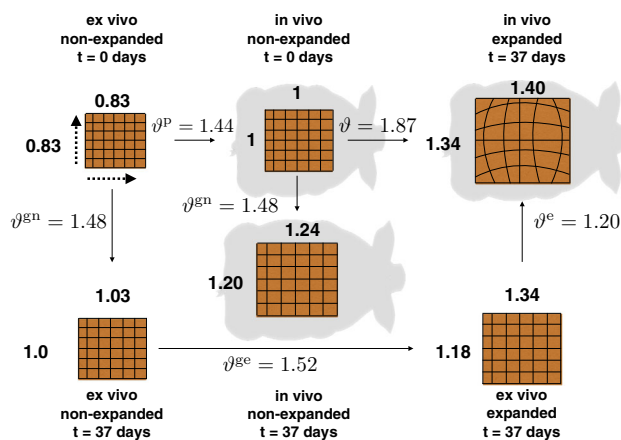


Fig. 7 Distinct configurations of the skin patch. Upon explantation, an in vivo unit square retracts to a square of dimensions 0.83×0.83 due to prestrain. Upon expansion, the unit square transforms into a 1.40×1.34 rectangle, with greater stretch in the direction parallel to the midline. During expansion, the patch grows naturally by 1.24×1.20 . The final size of the expanded patch includes natural and expander-induced growth, which turns a 1.03×1.00 naturally grown patch into the final 1.34×1.18 ex vivo patch

Table 1 Summary of prestrain for patch S

Prestrain measure	Ex vivo non-expanded $t = 37$ days	In vivo non-expanded $t = 37$ days
$\vartheta_{avg}^P [-]$	1.00	1.44
$\vartheta_{max}^P [-]$	1.00	2.37
$\vartheta_{min}^P [-]$	1.00	0.63
$\lambda_{1,avg}^P [-]$	1.00	1.21
$\lambda_{1,max}^P [-]$	1.00	1.62
$\lambda_{1,min}^P [-]$	1.00	0.70
$\lambda_{2,avg}^P [-]$	1.00	1.21
$\lambda_{2,max}^P [-]$	1.00	1.54
$\lambda_{2,min}^P [-]$	1.00	0.91
Error e [%]	13.10	2.00

animal is sacrificed, once of the excised tissue. The deformation map between these two configurations, indicated as F^P in Fig. 6, defines the area change due to prestrain at every point across the grid. We assume the excised tissue to be stress free and label the total deformation of skin in vivo as F^P . We calculate the local area change as $\vartheta^P = \det(F^P)$. We quantify the average area change as $\vartheta_{avg}^P = 1.44$, with maximum and minimum values of $\vartheta_{max}^P = 2.37$ and $\vartheta_{min}^P = 0.63$. We calculate the prestretch in the directions of the covariant basis vectors G_1 and G_2 , which correspond to the sagittal and transverse directions. The prestretches average $\lambda_1^P = 1.21$ and $\lambda_2^P = 1.21$. Table 1 summarizes the results of the prestrain analysis. Figure 8 illustrates the contour plots of the total area prestrain ϑ^P as well as the prestretches λ_1^P and λ_2^P

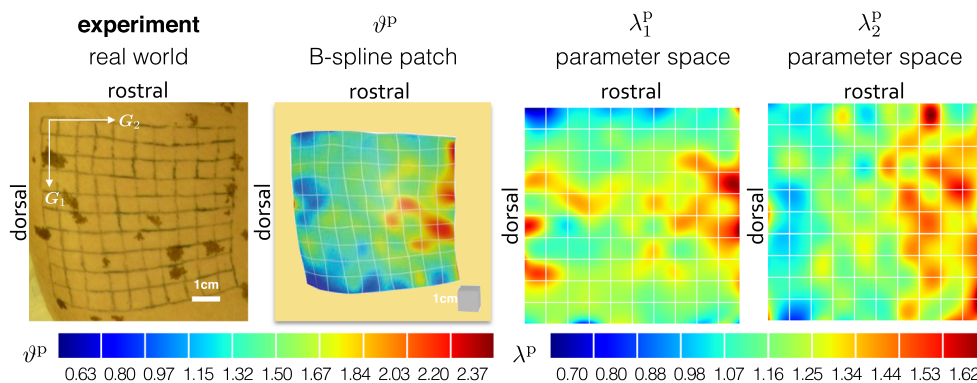


Fig. 8 Prestrain. The *first column* shows the experimental setup. The *second column* shows the geometric representation using a B-spline patch with the overlaid contour plot of the total area change ϑ^P , which averages 1.44. The *third and fourth columns* show the contour plots of

the anisotropic prestretches λ_1^P and λ_2^P in the directions parallel and perpendicular to the midline, both directions exhibit average values 1.21

Table 2 Summary of deformation for patch R

Time [days]	Volume [cc]	ϑ_{avg} [-]	ϑ_{max} [-]	ϑ_{min} [-]	$\lambda_{1,\text{avg}}$ [-]	$\lambda_{1,\text{max}}$ [-]	$\lambda_{1,\text{min}}$ [-]	$\lambda_{2,\text{avg}}$ [-]	$\lambda_{2,\text{max}}$ [-]	$\lambda_{2,\text{min}}$ [-]	Error e [%]
0	0	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	4.7
0	50	1.17	2.49	0.41	1.13	2.24	0.52	1.04	2.23	0.45	0.9
8	100	1.31	2.79	0.50	1.19	2.08	0.43	1.10	2.16	0.60	1.0
15	150	1.43	3.21	0.33	1.22	2.29	0.38	1.17	2.58	0.49	1.0
22	200	1.73	4.08	0.46	1.40	2.64	0.39	1.24	2.89	0.70	1.5
29	250	1.77	3.52	0.48	1.36	2.30	0.48	1.29	2.71	0.55	1.2
35	280	1.87	4.05	0.53	1.39	2.43	0.41	1.34	2.72	0.55	0.6

parallel to the dorsal midline and perpendicular to the dorsal midline along the skin tension lines.

3.2 Deformation

Figure 7 summarizes the result of the deformation analysis with the non-expanded in vivo patch R at day $t = 0$ as reference configuration. Every week, we obtain the deformation of the patch with respect to the reference configuration and calculate the corresponding gradient F . We are interested in the total area change ϑ and two in-plane stretches λ_1 and λ_2 parallel and perpendicular to the midline. Table 2 summarizes the results of the weekly inflations.

The average area stretch increases monotonically with each inflation, reaching a final value of $\vartheta_{\text{avg}} = 1.87$ with respect to the non-expanded reference patch at day $t = 0$. The stretches in the directions parallel and perpendicular to the midline display an interesting trend: The stretch perpendicular to the midline λ_2 is always smaller than the corresponding parallel stretch λ_1 . This implies that the tissue is stretched more parallel than perpendicular to the long axis of the animal. After the expansion process is complete, the average stretches are $\lambda_{1,\text{avg}} = 1.40$ and $\lambda_{2,\text{avg}} = 1.34$. This

deformation corresponds to a unit square stretched to a rectangle of dimensions 1.40×1.34 as illustrated in Fig. 7.

Figure 9 shows the contour plots of the total area stretch ϑ and the stretches λ_1 and λ_2 parallel and perpendicular to the midline. The total deformation is greater in the center of the expander and it decreases toward the edges of the patch. The stretches λ_1 parallel to the midline shows a similar distribution to the total area stretch. The stretches λ_2 perpendicular to the midline show slightly higher values near the center of the expander, but their overall contour profile appears to be more homogeneous.

3.3 Growth

While the expansion process is taking place, the animal undergoes natural growth. We quantify the total physiological growth comparing the control patch S at days $t = 0$ and $t = 37$ before the animal is sacrificed. The gradient of the deformation between these two configurations, F^{gn} , is illustrated in Fig. 6. The natural area growth is $\vartheta^{\text{gn}} = \det(F^{\text{gn}})$. On average, skin grows naturally by $\vartheta_{\text{avg}}^{\text{gn}} = 1.49$. Remarkably, growth is anisotropic averaging $\lambda_{1,\text{avg}}^{\text{gn}} = 1.24$ and

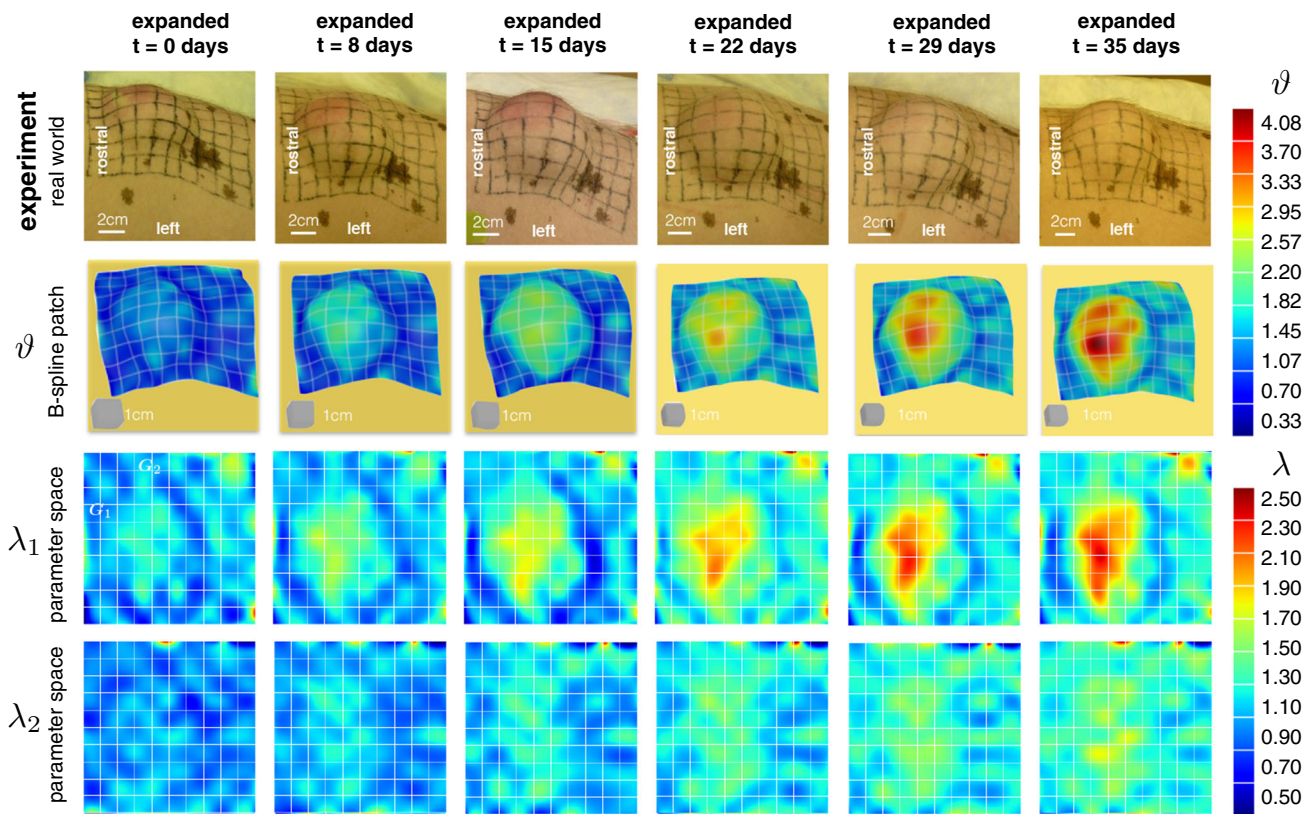


Fig. 9 Deformation. The *columns* depict the chronic overstretch due to weekly inflations. The *first row* shows photographs of the experimental setup at different points in time. Sets of photographs at each time point allow us to reconstruct the B-spline patches in the *second row*.

We are interested in the total area change ϑ as well as stretches λ_1 and λ_2 parallel and perpendicular to the midline. The contour plots reveal larger strains at the center of the expander and smaller strains in the periphery

$\lambda_{2,avg}^{gn} = 1.20$ parallel and perpendicular to the midline. Graphically, natural growth can be visualized as a unit square turned into a rectangle of dimensions 1.24×1.20 drawn in Fig. 7. Table 3 compiles these findings.

In response to deformations beyond the physiological limits, skin grows to re-establish a state of mechanical homeostasis. At the end of the expansion procedure, the excised, expanded tissue patch partially retracts and exposes the reversible, purely elastic part of the deformation F^e . We create kinematic representations of the patch R at day $t = 37$, both in vivo and ex vivo. The determinant of deformation gradient F^e between these two configurations defines the elastic area change, which averages $\vartheta_{avg}^e = 1.20$. The elastic stretches parallel and perpendicular to the midline are $\lambda_{1,avg}^e = 1.05$ and $\lambda_{2,avg}^e = 1.14$. Table 4 collects these results.

The remaining deformation of the expanded patch contains the information related to skin growth. The total area growth can itself be understood as the multiplicative decomposition into natural growth and expansion-induced growth, $F^g = F^{ge} \cdot F^{gn}$. Following the diagram in Fig. 6, we can compute the total growth using the prestrain, natural

Table 3 Summary of natural growth for patch S

Growth	In vivo non-expanded $t = 0$ days	In vivo non-expanded $t = 37$ days
$\vartheta_{avg}^{gn} [-]$	1.00	1.48
$\vartheta_{max}^{gn} [-]$	1.00	2.36
$\vartheta_{min}^{gn} [-]$	1.00	1.07
$\lambda_{1,avg}^{gn} [-]$	1.00	1.24
$\lambda_{1,max}^{gn} [-]$	1.00	1.57
$\lambda_{1,min}^{gn} [-]$	1.00	0.78
$\lambda_{2,avg}^{gn} [-]$	1.00	1.20
$\lambda_{2,max}^{gn} [-]$	1.00	1.83
$\lambda_{2,min}^{gn} [-]$	1.00	0.95
error e [%]	2.07	2.00

growth, and elastic deformation tensors already available, then $F^g = F^{e-1} \cdot F \cdot F^p$.

The average total area growth is $\vartheta_{avg}^g = 2.25$, of which $\vartheta_{avg}^{ge} = 1.52$ can be attributed exclusively to expansion-induced growth. The average total growth parallel and per-

Table 4 Summary of purely elastic deformation for patch R

Elastic deformation	Ex vivo expanded $t = 37$ days	In vivo expanded $t = 37$ days
ϑ_{avg}^e [–]	1.00	1.20
ϑ_{max}^e [–]	1.00	2.52
ϑ_{min}^e [–]	1.00	0.63
$\lambda_{1,\text{avg}}^e$ [–]	1.00	1.05
$\lambda_{1,\text{max}}^e$ [–]	1.00	1.63
$\lambda_{1,\text{min}}^e$ [–]	1.00	0.61
$\lambda_{2,\text{avg}}^e$ [–]	1.00	1.14
$\lambda_{2,\text{max}}^e$ [–]	1.00	2.02
$\lambda_{2,\text{min}}^e$ [–]	1.00	0.65
Error e [%]	1.7	0.6

Table 5 Summary of total growth, natural growth, and expansion-induced growth, from analyzing patches R and S

Growth	Avg	Max	Min
ϑ^g [–]	2.25	4.81	0.52
ϑ^{gn} [–]	1.48	2.36	1.07
ϑ^{ge} [–]	1.54	3.30	0.28
λ_1^g [–]	1.62	3.24	0.61
λ_1^{gn} [–]	1.24	1.57	0.78
λ_1^{ge} [–]	1.31	2.65	0.43
λ_2^g [–]	1.43	2.98	0.57
λ_2^{gn} [–]	1.20	1.83	0.95
λ_2^{ge} [–]	1.19	2.61	0.40

pendicular to the midline is $\lambda_{1,\text{avg}}^g = 1.62$ and $\lambda_{2,\text{avg}}^g = 1.43$. Again, we can deduce the amount of natural growth to obtain the average expansion-induced growth $\lambda_{1,\text{avg}}^{\text{ge}} = 1.31$ and $\lambda_{2,\text{avg}}^{\text{ge}} = 1.19$. Growth of a unit square is anisotropic, both natural growth and expansion-induced growth induce a larger tissue gain parallel to the midline. Table 5 summarizes these findings. Figure 10 shows the contour plots of the three different growth quantities.

4 Discussion

Skin grows in response to chronic overstretch: At the end of a tissue expansion procedure, the total deformation is a combination of reversible and irreversible contributions. Plastic and reconstructive surgeons typically guess the time point, by which they have expanded the tissue enough to create a sufficiently large patch for defect correction. In clinical practice, this lack of knowledge leads to severe and unnecessary overgrowth.

Here we extend our novel experimental setup (Buganza Tepole et al. 2014) toward a new anisotropic characterization of prestrain, deformation, and growth using a porcine skin expansion model. We combine two recent technologies, multi-view stereo (MVS) and isogeometric analysis (IGA), within the continuum theory of finite growth. MVS allows us to reconstruct three-dimensional models from a set of uncalibrated photographs with unknown camera positions. Isogeometric analysis uses B-spline basis functions to smoothly interpolate surface deformation maps and strain fields over relatively coarse meshes. The theory of finite growth captures reversible and irreversible deformation by splitting the total deformation gradient into an elastic and a growth part. Here we are specifically interested in quantifying three aspects of the expansion process: prestrain, deformation, and growth.

We find that skin in vivo is prestretched isotropically, on average by $\vartheta^p = 1.44$, i.e., by $\lambda^p = 1.21$ parallel and perpendicular to the midline. Ventral porcine integument has revealed prestretch on the same order of magnitude, with average in vivo stretches of 1.26 transversely and 1.65 longitudinally (Jor et al. 2010). Experiments on human forearm skin displayed similar values with an almost isotropic area prestrain on the order of 1.57 (Flynn et al. 2011). The quantification of isotropic prestrain is thought-provoking: While skin is clearly anisotropic, this does not necessarily imply that prestrain has to be anisotropic as well. Human skin in the forearm displayed similar prestrain values in two orthogonal directions (Flynn et al. 2011), while ventral pig skin exhibited marked anisotropic prestrain (Jor et al. 2010). Unfortunately, the purely kinematic analysis of our experimental setup fails to shed light on the morphogenetic processes that explain the observed prestrain patterns. However, throughout our expansion protocol, we have also performed biochemical assays including the immunohistochemistry in Fig. 11, which we are currently analyzing with the objective to correlate biochemical and mechanical phenomena and reveal directional information.

By subcutaneously implanting an expander underneath a 10×10 cm grid and filling it gradually up to 280 cc, the overlying skin is chronically stretched beyond its physiological limit (Buganza Tepole et al. 2012). At the end of five weekly timed inflations, the initial patch is stretched on average by 1.40×1.34 parallel and perpendicular to the midline, respectively. It is interesting to highlight the anisotropy of the resulting deformation. Just like most soft biological tissues, skin is known to exhibit anisotropic material properties (Lanir 1983). In fact, Langer mapped the preferred stiffness directions of skin over the human body more than a century ago (Langer 1861). Tension lines in the pig have been characterized in great detail (Rose et al. 1976). Uniaxial tension tests of rabbit skin and biaxial testing of porcine skin have initiated the development of microstructurally based anisotropic material constitutive laws (Jor et al. 2010; Tong and Fung

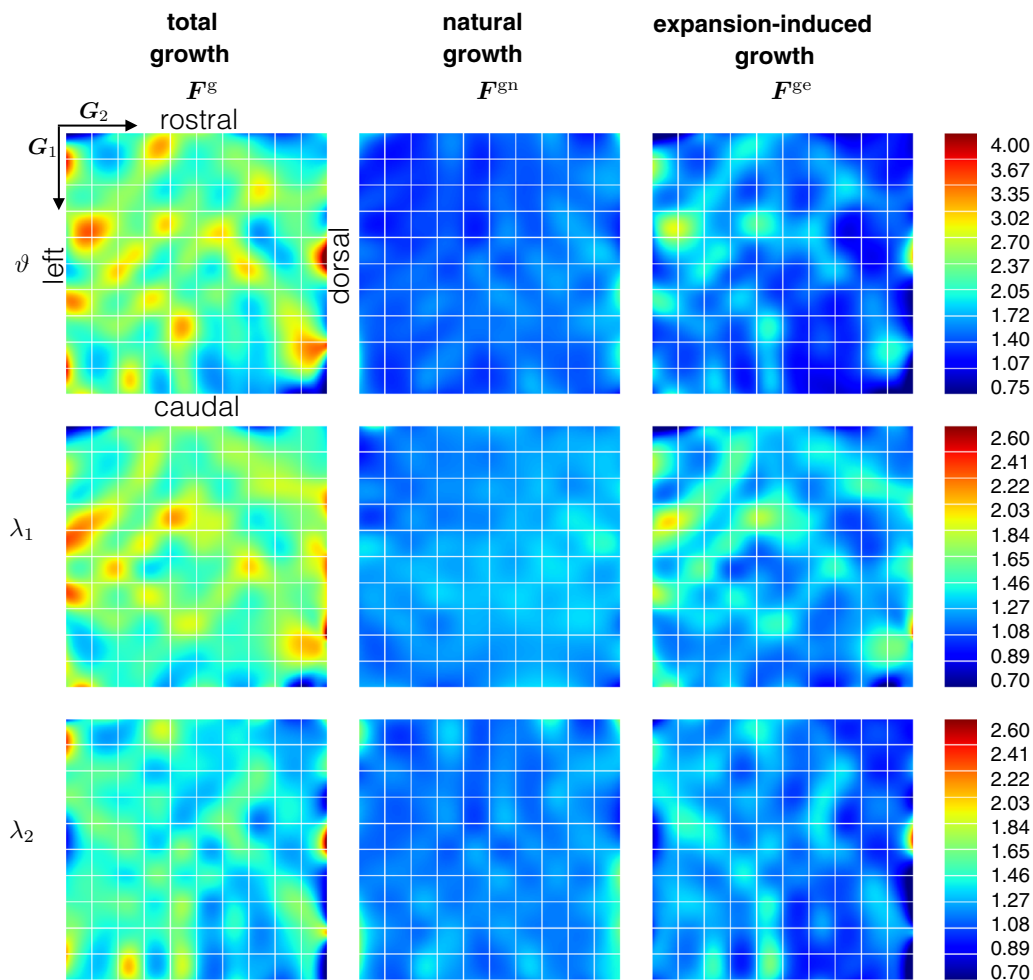


Fig. 10 Growth. Total, natural, and expansion-induced growth are calculated from prestrain, total deformation, and elastic deformation. The columns show the decomposition of the total growth tensor F^g into natural growth F^{gn} and expansion-induced growth F^{ge} . The rows show-

case the total area growth ϑ^g and the corresponding growth stretches λ_1^g and λ_2^g parallel and perpendicular to the midline. Natural growth is more homogeneous than expansion-induced growth, which is larger in regions where the overall deformation is larger

1976). It seems reasonable that the anisotropic microstructure of skin induces anisotropic deformation upon pressure-induced expansion with smaller stretches along the skin tension lines (Menzel 2007). It is noteworthy that our maximum stretch values occur perpendicular to the midline, although on average, the general trend indicates the opposite. To further explore this phenomenon, our current and future efforts aim at tracking the collagen fiber arrangement before, during, and after tissue expansion using high-resolution ultrasound and immunohistochemistry. Figure 11 illustrates our first attempts along these lines, which will eventually allow us to correlate skin growth to cellular and subcellular phenomena including cell proliferation.

At the culmination of the expansion process, on day $t = 37$, the total deformation is a combination of growth and elastic components. We excise the expanded tissue to

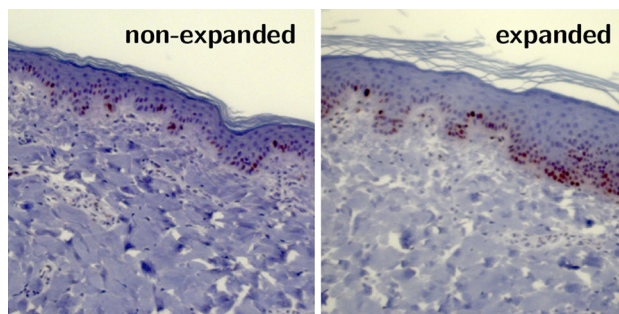


Fig. 11 Representative tissue sections of non-expanded and expanded skin immunostained for Ki-67, a nuclear protein associated with cell proliferation. The control skin patch, left, displays a normal epidermal thickness and a normal number of dividing cells. The expanded skin patch, right, shows an increase in epidermal thickness and an increased number of dividing cells indicating skin growth. In both sections, the dermis displays a diffuse collagen orientation

quantify the elastic contribution and observe that the average area change is $\vartheta^e = 1.20$. A square region retracts 0.95×0.88 parallel and perpendicular to the midline. This finding is intriguing. From our prestrain quantification, we conclude that if we excise the original *in vivo* patch before expansion, it shrinks to a square of dimensions 0.83×0.83 . A possible explanation for the mismatch between elastic deformations before and after expansion is that the morphogenetic processes that result in the stable $\vartheta^p = 1.44$ area stretch *in vivo* are different from the equilibrium resulting from tissue expansion. Another plausible hypothesis is that the grown skin has not yet fully recovered its homeostatic equilibrium state. We plan to follow up expanded skin patches for longer time periods to determine the final equilibrium state of the expanded tissue.

Accounting for prestrain and elastic retraction, we calculate the resulting tissue growth. On average, tissue grows by $\vartheta^g = 2.25$ in area. We find, once more, that skin kinematics are different in the two directions of interest. An *ex vivo* unit square at day $t = 0$ transforms into a 1.62×1.43 rectangle *ex vivo* after $t = 37$ days of expansion. Growth also shows a distinct regional variation. As we would intuitively expect, growth is largest in the center region, which experiences the largest stretch. This supports the hypothesis that overstretch drives skin growth (Zöllner et al. 2012). Several factors can explain the regional variation parallel and perpendicular to the midline. First, we find that while the expansion takes place the skin patch grows naturally in an approximately homogeneous, yet anisotropic manner on average by 1.24×1.20 times. From our contour plots, we can also observe that the deformation induced by expansion is greater in the parallel direction. Nonetheless, there is still debate whether microstructural cues, such as the arrangement of the collagen architecture, guide anisotropic growth. This question also motivates further experiments.

Our study has a few limitations. We recognize that there is no one-to-one correspondence between the material properties and anatomies of porcine and human integument. Another limitation is that we have only performed this study at a single location in a single porcine model. Nonetheless, we believe that our results provide promising evidence for our experimental design and prompt us to replicate the analysis in a larger group. Toward these efforts, we are currently designing instrumented expanders to measure the expander pressure before and after expansion (Pamplona and Mota 2012). This will eventually allow us to characterize the stiffness of living skin stiffness using an inverse finite element approach (Pamplona and Carvalho 2012). The shape of the expander could also bias the resulting deformation contours (Buganza Tepole et al. 2011). We are therefore replicating the experiment on a larger sample set to account for different expander geometries and to demonstrate statistical significance of our results.

Taken together, we presented a highly flexible experimental setting to accurately track surface kinematics using multi-view stereo. Multi-view stereo is a robust, inexpensive, non-invasive technology that can be readily used in plastic and reconstructive surgery, where skin is conveniently exposed to the outside world. Performing numerical analysis within the isogeometric setting resolves rich regional variations, which could ultimately lead to address and propose more fundamental questions. Indeed, in this manuscript, we start from a particular medical application, skin expansion, a widely used reconstructive technique. An accurate kinematical characterization of tissue expansion could improve preoperative planning and optimize treatment options. When combined with histological and biochemical essays at smaller scales, our continuum interpolation of mechanical fields has the potential to uncover mechanotransduction pathways in living skin and inspires us to manipulate biological membranes by mechanical stretch.

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