Kinematics

Despite tremendous research during the past 20 years, heart failure remains one of the most common, costly, disabling, and deadly medical conditions affecting more than 25 million people worldwide. In an attempt to better understand heart disease and to quantify strain profiles in the beating heart, researchers in the lab of Prof. D. Craig Miller in the Department of Cardiothoracic Surgery in the School of Medicine at Stanford have developed a novel technique to measure infarct-induced changes of ventricular wall kinematics. They insert a transmural beadset into the wall of the heart, see Figure 1, and acquire videofluoroscopic images at 60 frames per second using a biplane videofluoroscopy system. To obtain a fully three-dimensional picture of the deformation, they merge the marker coordinates from two biplane views using semi-automated image processing and digitization software. To determine local muscle fiber directions, they cut transmural rectangular blocks of tissue from the regions with the implanted markers and slice them into 1mm thick transmural sections. This allows them to measure the muscle fiber orientation at each point through tissue histology. The objective of this homework is to quantify ventricular wall strains and characterize muscle fiber contraction in vivo using these experimental data. This homework can help to answer the following scientific and clinical questions: Does fiber contraction display regional and transmural variations? How do contraction profiles change in regions close to an infarct? Can passive support prevent these changes? Is the fiber contraction of the non-infarcted myocardium inherently normal? Does the failing heart dilate uniformly or is dilation distributed heterogeneously?
Figure 2 shows a typical data set of four markers of the beadset array. The red tetrahedron shows the marker positions \( X \) at end diastole, i.e., at the end of the cardiac filling phase. The blue tetrahedron illustrates the marker positions \( x \) at end systole, i.e., at the end of the cardiac contraction phase. You can assume that the tetrahedra in Figure 2 are oriented such that their \( e_3 \) (or \( z \)) axis is aligned with in the longitudinal direction of the heart, and that \( e_1 \) (or \( x \)) and \( e_2 \) (or \( y \)) are the radial/transmural and circumferential directions, respectively. Just to give you an idea, the left ventricular chamber is about 8 cm long and has a maximum radius of approximately 4 cm. The measured marker coordinates are given below.

\[
\begin{align*}
X_0 &= \begin{bmatrix} +0.25 & -0.27 & -0.25 \end{bmatrix}^t \\
X_1 &= \begin{bmatrix} +0.25 & +0.53 & -0.25 \end{bmatrix}^t \\
X_2 &= \begin{bmatrix} -0.05 & +0.52 & -0.25 \end{bmatrix}^t \\
X_3 &= \begin{bmatrix} +0.25 & +0.13 & +0.45 \end{bmatrix}^t \\
x_0 &= \begin{bmatrix} +0.01 & -0.40 & +0.15 \end{bmatrix}^t \\
x_1 &= \begin{bmatrix} +0.00 & +0.32 & +0.15 \end{bmatrix}^t \\
x_2 &= \begin{bmatrix} -0.33 & +0.38 & +0.21 \end{bmatrix}^t \\
x_3 &= \begin{bmatrix} +0.05 & +0.07 & +0.85 \end{bmatrix}^t
\end{align*}
\]

The histologically measured fiber orientation angle for the displayed tetrahedra, measured clockwise against the horizontal axes, is \( \alpha = 45.4^0 \), indicated through the two black lines in Figure 2. For simplicity, you can assume that the muscle fibers are planar in the transmural plane. The cardiac muscle fiber direction \( N^{fib} \) in the relaxed diastolic configuration is thus given through the following unit vector.

\[
N^{fib} = \begin{bmatrix} 0.0 & -\cos(\alpha) & +\sin(\alpha) \end{bmatrix}^t \quad \text{with} \quad \alpha = 45.4^0
\]

The overall objective is this homework is to determine the muscle fiber contraction in a beating heart. This is pretty straightforward if you solve the following substeps.

[1] **Determine three vectors \( dX_i \) that span the tetrahedron at end diastole.**

Take an arbitrary point of the tetrahedron as origin, e.g., \( X_0 \), and calculate the three vectors \( dX_1, dX_2, \) and \( dX_3 \) from the origin to any other point using the coordinates \( X \) at end diastole such that \( dX_i = X_i - X_0 \) for \( i = 1, 2, 3 \).

[2] **Determine the same three vectors \( dx_i \) that span the tetrahedron at end systole.**

Take the same point as origin, e.g., \( x_0 \), and calculate the vectors \( dx_1, dx_2, \) and \( dx_3 \) from the origin to any other point using the coordinates \( x \) at end systole such that \( dx_i = x_i - x_0 \) for \( i = 1, 2, 3 \).

[3] **Determine the deformation gradient tensor \( F \) that maps all diastolic line elements as \( dX_i \) onto the systolic line elements \( dx_i \).**

\( F = \frac{\partial x}{\partial X} \) is called the deformation gradient and it is the key kinematic quantity to characterize finite strain kinematics. It maps line elements according to \( dx_i = F \cdot dX_i \).
Applying this mapping to all three line elements $\text{d}X_i$ defines three vector valued equations, i.e., nine equations to solve for the nine components of $F$. To obtain a more compact notation, rearrange all diastolic line elements from [1] and all systolic line elements from [2] in $3 \times 3$ matrices $\mathbf{C} := [\text{d}X_1; \text{d}X_2; \text{d}X_3]$ and $\mathbf{c} := [\text{d}x_1; \text{d}x_2; \text{d}x_3]$. Now, determine the deformation gradient $F$ by solving the equation $F \cdot \mathbf{C} = \mathbf{c}$.

[4] Control your results by calculating $\text{d}x_i = F \cdot \text{d}X_i$.

Do the calculated systolic line elements $\text{d}x_i$ match the ones you had calculated in [2]?

[5] Determine the systolic fiber direction $n_{fib} = F \cdot N_{fib}$.

The deformation gradient can be used to map the measured diastolic fiber direction $N_{fib}$ onto the systolic fiber direction $n_{fib}$. Determine $n_{fib}$ and comment on how $N_{fib}$ and $n_{fib}$ deviate.

[6] Determine the fiber stretch $\lambda = \sqrt{n_{fib} \cdot n_{fib}}$.

Since the fiber orientation $N_{fib}$ was given as a unit vector, the length of the systolic vector $n_{fib} = F \cdot N_{fib}$ corresponds to the relative change in fiber length, i.e., the fiber stretch in the finite strain setting, $\lambda = \sqrt{n_{fib} \cdot n_{fib}} = \sqrt{N_{fib} \cdot F \cdot F \cdot N_{fib}}$.

[7] Determine the second order Green Lagrange strain tensor $E = \frac{1}{2} [F' \cdot F - I]$.

$E$ is called the Green Lagrange strain tensor and it is used to characterize strains in the undeformed configuration in a finite strain setting.

[8] Determine the displacement gradient tensor $H = F - I$.

$H = \nabla u$ is the nonsymmetric displacement gradient tensor which can also be expressed as $H = \frac{\partial u}{\partial x} = \frac{\partial [x - X]}{\partial X} = F - I$.

[9] Linearize the Green Lagrange strain tensor $E$ with the help of the Gateaux derivative to obtain the small strain tensor $\epsilon = \frac{1}{2} (H + H')$.

Linearize $E$ formally, then calculate $\epsilon$, compare the small strain approximation $\epsilon$ with the large strain Green Lagrange tensor $E$, and comment on your results.

[10] Determine the volume dilation $e = \text{tr}(\epsilon)$.

Comment on whether the tissue behaves compressible or incompressible and on whether this was what you would have expected.

[11] Last, determine the normal strain $\epsilon_n = N_{fib} \cdot \epsilon \cdot N_{fib}$. Compare the large strain fiber stretch $\lambda$ to the small strain approximation of the fiber contraction $\epsilon_n$. Comment on your results. Do you think they are reasonable? Find evidence in the literature about the amount of maximum cardiomyocyte contraction.

You can use MATLAB to solve the matrix and vector operations. If you choose to do so, you must deliver a printout of your MATLAB code with the homework.

Research paper

Active contraction of cardiac muscle: In vivo characterization of mechanical activation sequences in the beating heart

Alkiviadis Tsamis\textsuperscript{a}, Wolfgang Bothe\textsuperscript{b}, John-Peder Escobar Kvitting\textsuperscript{b}, Julia C. Swanson\textsuperscript{b}, D. Craig Miller\textsuperscript{b}, Ellen Kuhl\textsuperscript{a,b,c,*}

\textsuperscript{a}Department of Mechanical Engineering, 496 Lomita Mall, Stanford, CA-94305, USA
\textsuperscript{b}Department of Cardiothoracic Surgery, 300 Pasteur Drive, Stanford, CA-94305, USA
\textsuperscript{c}Department of Bioengineering, 496 Lomita Mall, Stanford, CA-94305, USA

\textbf{Article history:}
Received 22 January 2011
Received in revised form 22 March 2011
Accepted 29 March 2011
Published online 7 April 2011

\textbf{Keywords:}
Biomechanics
Cardiac mechanics
Muscle
Excitation
Contraction
Transmural strains

\textbf{Abstract}
Progressive alterations in cardiac wall strains are a classic hallmark of chronic heart failure. Accordingly, the objectives of this study are to establish a baseline characterization of cardiac strains throughout the cardiac cycle, to quantify temporal, regional, and transmural variations of active fiber contraction, and to identify pathways of mechanical activation in the healthy beating heart. To this end, we insert two sets of twelve radiopaque beads into the heart muscle of nine sheep; one in the anterior-basal and one in the lateral-equatorial left ventricular wall. During three consecutive heartbeats, we record the bead coordinates via biplane videofluoroscopy. From the resulting four-dimensional data sets, we calculate the temporally and transmurally varying Green–Lagrange strains in the anterior and lateral wall. To quantify active contraction, we project the strains onto the local muscle fiber directions. We observe that mechanical activation is initiated at the endocardium slightly after end diastole and progresses transmurally outward, reaching the epicardium slightly before end systole. Accordingly, fibers near the outer wall are in contraction for approximately half of the cardiac cycle while fibers near the inner wall are in contraction almost throughout the entire cardiac cycle. In summary, cardiac wall strains display significant temporal, regional, and transmural variations. Quantifying wall strain profiles might be of particular clinical significance when characterizing stages of left ventricular remodeling, but also of engineering relevance when designing new biomaterials of similar structure and function.

© 2011 Elsevier Ltd. All rights reserved.

1. Introduction

Repairing the failing heart is a desirable but elusive goal. Despite tremendous scientific progress during the past decades, heart failure remains one of the most common, costly, disabling, and deadly medical conditions affecting more than 25 million people worldwide (Lloyd-Jones et al., 2010). Dilation of the left ventricle, change in ventricular shape, and
decrease in ejection fraction are clinical indicators of disease progression and strong predictors of survival (Gaudron et al., 1993). Effective therapies for heart failure seek to attenuate these effects and reverse disease progression (McGee et al., 2006). Particularly promising examples are biomaterial approaches that seek to support the ventricular wall to reduce stress and alleviate cardiomyocyte overstretch (Christman and Lee, 2006). Research in biomaterials currently focuses on three mechanisms of wall support: The injection of living cells into the myocardium to create in situ engineered cardiac tissue (Wollert et al., 2004); the implantation of in vitro engineered tissue patches (Böl et al., 2009; Leong et al., 2008); and the implantation of synthetic patches or passive cardiac support devices around the heart (Cheng et al., 2006b). The objective of this study is to provide guidelines for the structural and functional requirements of these biomaterial solutions. In particular, we seek to establish a baseline characterization of cardiac and fiber strains throughout the cardiac cycle, to quantify temporal, regional, and transmural variations of active muscle contraction, and to identify pathways of mechanical activation in the healthy beating heart. This baseline characterization of cardiac strains is also of clinical significance since it may help to judge strain alterations in response to cardiac disease.

For more than 30 years, the use of implanted radiopaque markers has provided considerable insight into the complex transmural dynamics of the healthy and diseased ventricular myocardium. In the first series of experiments, small lead spheres were inserted with a needle into the anterior left ventricular wall of five canine hearts to characterize the complex transmural deformation pattern using biplane cineradiography (Fenton et al., 1978). Ventricular wall strains were extracted from the experimentally measured marker coordinates using the field theories of continuum mechanics. While the data analysis was initially based on the assumption of infinitesimal deformations, subsequent studies demonstrated the need to extend the analysis to finite deformations (Waldman et al., 1985). Over the years, the bead insertion technique was refined and standardized to the method we have adopted within this study (Cheng et al., 2005a; Waldman et al., 1985). One of the major breakthroughs enabled by the transmural marker technique was to precisely quantify how individual strain components change with depth, from the epicardium, the outer wall, to the endocardium, the inner wall. While the earlier studies used a discrete point-wise representation of strains, refined methods now use a continuous functional representation, either in the form of fitted bilinear cubic finite elements (McCulloch and Omens, 1991) or fitted polynomials (Kindberg et al., 2007), the method we adopt here. In combination with tissue histology, this functional representation naturally lends itself to the quantification of fiber and sheet strains which have significantly improved our understanding of the mechanics underlying coordinated pump function (Arts et al., 2001; Cheng et al., 2005b, 2008; Costa et al., 1999).

Throughout the past two decades, marker-based strain characterization has been used both in canine (Arts et al., 2001; Costa et al., 1999; McCulloch and Omens, 1991; Waldman et al., 1985) and ovine (Carhäll et al., 2008; Cheng et al., 2005a,b, 2006a; Kindberg et al., 2007) hearts, with generally similar results, however, strains being slightly larger in dogs than in sheep. The marker technique has been used successfully to identify the impact of acute changes in strain profiles, for example initiated by varying afterload (Takayama et al., 2002) or by ventricular pacing (Coppola et al., 2007). However, the true beauty of this technique lies in its permanent nature allowing to precisely quantify chronic changes, for example in response to mitral regurgitation (Carhäll et al., 2008) or myocardial infarction, in its plain form, or treated with a passive support device (Cheng et al., 2006a). Overall, this technique is relatively well-known in the surgical community but less so in the engineering community. One of the goals of this manuscript is therefore to discuss this technique in view of a modern continuum mechanics analysis which allows us to reconstruct the tensorial characterization of ventricular wall kinematics.

Most existing marker studies use the end-diastolic state as the reference configuration and the end-systolic state as the deformed configuration. Accordingly, they fail to give a complete picture of the spatio-temporal strain evolution across the ventricular wall. Using a novel time-aligned averaging technique to create a functional representation of the underlying Green–Lagrange strains (Rausch et al., 2011, in press), we reconstruct strain profiles throughout the entire wall throughout the entire cardiac cycle averaged over nine animals. This allows us to visualize the mechanical activation sequence across the ventricular wall. The resulting color-coded graphics demonstrate that maximum fiber contraction may in fact occur significantly after the end-systolic state.

2. Materials and methods

We premedicate nine adult male dorsett-hybrid sheep with ketamine, anesthetize them with sodium thiopental, intubate and ventilate them, and maintained general anesthesia with inhalational isoflurane and supplemental oxygen. After performing a left thoracotomy, we measure the wall thickness at the anterior-basal and at the lateral-equatorial regions of the left ventricular wall using epicardial echocardiography. At each of these two regions, we insert three transmural columns of four bead sets each (Waldman et al., 1985); see Fig. 1. Using a depth-adjustable bead insertion trocar, we first insert three 0.7 mm diameter beads in each column, evenly spaced between the endo- and epicardial surfaces. In addition, we sew a fourth 1.7 mm diameter bead onto the epicardial surface above each column. To access the left ventricular volume, we implant thirteen evenly spaced epicardial markers silhouetting the left ventricle. Before taking the animals to the catheterization laboratory for data acquisition, we place an implantable micromanometer pressure transducer in the left ventricular chamber and a micromanometer catheter into the ascending aorta for ventricular and aortic pressure measurements. During baseline conditions with the heart in normal sinus rhythm and the animals in the right lateral decubitus position, we record videofluoroscopic images of all beads and markers using biplane videofluoroscopy at a sampling frequency of 60 Hz. We simultaneously record aortic pressure, left ventricular pressure, and electrocardiogram voltage signals.
Using a semi-automated image processing and digitization software developed in our laboratory (Niczyporuk and Miller, 1991), we obtain three-dimensional coordinates \( x(X, t) \) of the four by three beads of both bead sets and of the thirteen left ventricular markers offline from the acquired biplane images. The accuracy of our three-dimensional displacement reconstruction from biplane videofluoroscopy is 0.1±0.3 mm (Daughters et al., 1989).

3. Theory and calculation

3.1. Cardiac coordinates

To create a functional representation of the strain field in the anterior-basal and lateral-equatorial wall, we define a local Cartesian coordinate system \( \{e_x, e_y, e_z\} \) aligned with the local circumferential, radial, and longitudinal directions; see Fig. 1. We place its origin into the geometric center of three epicardic beads which define a plane tangential to the outer cardiac wall. The radial axis \( e_r \) is oriented normal to this tangential plane, with a positive outward direction. The circumferential axis \( e_c \) is introduced normal to the vector connecting the apex of the heart with the origin of the coordinate system and normal to the radial axis, pointing in the mathematically positive direction when viewing the heart from base to apex. The longitudinal axis \( e_l \) is defined normal to the radial and circumferential axes, \( e_l = e_r \times e_c \), with a positive direction from apex to base; see Fig. 1.

3.2. Temporal interpolation and data analysis

To create an average strain representation in the anterior-basal and lateral-equatorial wall, we map all nine experimental data sets into four time intervals between End Diastole, ED, End Isovolumic Contraction, EIC, End Systole, ES, and End Isovolomic Relaxation, EIR, as previously described (Rausch et al., 2011, in press). We select these characteristic time points semi-manually from the individual pressure-volume relationships, with the volume defined in terms of the thirteen silhouetting epicardic markers. Based on different average interval lengths, these four time intervals are further subdivided into five segments from ED to EIC, eleven segments from EIC to ES, seven segments from ES to EIR, and ten segments from EIR to ED, respectively. Within each of these four intervals, we perform a linear temporal interpolation between the experimentally acquired raw data points \( x(X, t) \) to create temporally aligned data sets of hemodynamic and kinematic data at the corresponding five, eleven, seven, and ten segment points, thus representing the cardiac cycle through \( t_n \) discrete time points with \( n = 1, \ldots, 33 \). Using these time-aligned data sets, we perform the strain calculations described in the following section to extract the means and standard deviations of the Green–Lagrange strain components \( E(X, t) \) and fiber strains \( E_{FF}(X, t) \) at 33 discrete time points throughout the cardiac cycle.

3.3. Spatial interpolation and cardiac strains

We assume that within the space enclosed by each bead set, the current placement \( \psi(X, t) \) of each material point \( X \) at each time \( t \) can be approximated by a time-dependent mapping \( \zeta_j(t) \) of the spatial interpolation \( N_j(X) \) in the reference configuration,

\[
\psi(X, t) = \sum_{j=1}^{n_{max}} \zeta_j(t)N_j(X) \tag{1}
\]

where \( I = 1, \ldots, n_{max} \) is the order of the approximation. In particular, at each of the \( J = 1, \ldots, n_{pnt} \) experimentally measured data points with \( n_{pnt} = 12 \), this implies that

\[
x_j(t) = \sum_{J=1}^{n_{pnt}} c_J(t)N_j(x_j) \tag{2}
\]

where \( x = [x_c, x_l, x_l] \) are the measured data points, \( c = [c_c, c_l] \) are the unknown coefficients at each discrete time point \( t \) associated with the circumferential, longitudinal, and radial directions, and \( N_j \) are the interpolation terms associated with the corresponding coordinates \( X \) of point \( J \) in the reference configuration, in our case, at end diastole. Following the literature (Kindberg et al., 2007), we choose a

---

**Fig. 1** Locations of transmural beadsets in the anterior-basal and lateral-equatorial left ventricular wall, left. Left ventricle with both beadsets silhouetted by thirteen epicardial markers, right. C, R, and L denote the axes of the local circumferential–radial–longitudinal coordinate system.
shows the temporal evolution of the averaged left ventricular pressure, LVV left ventricular volume, ED end diastole, EIR end isovolumetric relaxation, ES end systole, and EIC end isovolumetric contraction.

linear interpolation in the circumferential and longitudinal directions and a quadratic interpolation in the radial direction such that \( N_l \) can be expressed through the following \( n_{\text{app}} = 9 \) terms, \( N_l = \{x_1, x_2, x_3, x_4, x_5\} \), for the unknown coefficients \( c_{3}\ldots c_{9} \), and for the interpolation matrix \( N_{[9 \times 12]} = [N_l(x_1), \ldots, N_l(x_{12})] \). We solve this system for the unknown coefficient \( c(t) \) using the pseudo inverse of the interpolation matrix.

\[
\begin{align*}
\mathbf{x}(t) &= \mathbf{c}(t) \mathbf{N}_{[9 \times 12]} \\
\mathbf{c}(t)[3 \times 12] &= \mathbf{c}(t)[3 \times 9] \mathbf{N}_{[9 \times 12]}^{-1} \\
\end{align*}
\]

is overdetermined. In the above matrix representation of Eq. (2), we have introduced the notation for the measured coordinates of the data points \( x_{[3 \times 12]} = \{x_1, \ldots, x_{12}\} \), for the unknown coefficients \( c_{3}\ldots c_{9} \), and for the interpolation matrix \( N_{[9 \times 12]} = [N_l(x_1), \ldots, N_l(x_{12})] \). We solve this system for the unknown coefficient \( c(t) \) using the pseudo-inverse of the interpolation matrix.

\[
\mathbf{c}(t) = \mathbf{x}(t) \mathbf{N}_{[9 \times 12]}^{-1} \mathbf{N}_{[9 \times 12]} \mathbf{c}(t) + \mathbf{N}_{[9 \times 12]}^{-1} \mathbf{N}_{[9 \times 12]} \mathbf{c}(t)
\]

With the coefficients \( c(t) \) known at each discrete time point \( t \), we can evaluate the nonlinear deformation map \( \varphi(X, t) = \sum_{i=1}^{n_{\text{app}}} c_i(t) N_i(X) \) as introduced in Eq. (1). Accordingly, the deformation gradient \( F = \nabla \varphi \) takes the following functional representation,

\[
F(X, t) = \sum_{i=1}^{n_{\text{app}}} c_i(t) \nabla N_i(X)
\]

where \( \nabla (c) = \{\partial c, \partial \eta, \partial \eta(\cdot)\} \) denotes the spatial gradient with respect to the local cardiac coordinate system. The Green–Lagrange strain tensor in the cardiac coordinate system can then be expressed as follows.

\[
E(X, t) = \frac{1}{2} (F^T \cdot F - I)
\]

Using regionally and transmurally varying fiber directions reported in the literature (Ennis et al., 2008), we project the Green–Lagrange strain tensor onto the local fiber direction \( f(X) \),

\[
E_{FF}(X, t) = f(X) \cdot E(X, t) \cdot f(X)
\]

to characterize the local fiber strains \( E_{FF}(X, t) \). To illustrate the transmural variation of the cardiac strains and fiber strains, we evaluate Eqs. (6) and (7) for varying depths, i.e., along the radial direction \( X = \{0, 0, X_r\} \).

4. Results

4.1. Hemodynamics

Fig. 2 shows the temporal evolution of the averaged left ventricular pressure LVP and left ventricular volume LVV over the cardiac cycle, left, and the resulting averaged pressure–volume loop, right. The left ventricular pressure exhibits the characteristic n-shape with small standard deviations. The left ventricular volume remains virtually unchanged during isovolumetric contraction from ED to EIC, with an end-diastolic volume of 57.4 ± 10.5 mL. It decreases during ejection from EIC to ES, reaching an end-systolic volume of 43.9 ± 9.3 mL. Average stroke volume and average ejection fraction are 15 mL and 26%, respectively. Means and standard deviations are displayed for \( n = 9 \) animals to the top of the curve. LVP left ventricular pressure, LVV left ventricular volume, ED end diastole, EIR end isovolumetric relaxation, ES end systole, and EIC end isovolumetric contraction.

Fig. 3 summarizes the temporal evolution of the average cardiac strains in the anterior-basal left ventricular midwall, i.e., at 50% depth, at which the fiber direction is approximately aligned with the circumferential direction. The circumferential strains \( E_{CC} \) displayed on the top left are slightly tensile after end diastole with a maximum value of \( +2.0 \pm 1.7 \% \) at end isovolumetric contraction, then become compressive and decrease towards their minimum value of \( -7.9 \pm 3.8 \% \) at end isovolumetric relaxation, before returning back to zero at end diastole. The radial strains \( E_{RR} \) displayed on the bottom left behave in the opposite way. The wall thins slightly from end diastole towards \( -3.8 \pm 3.5 \% \) at end isovolumetric contraction, then thicken during systole towards \( +11.3 \pm 6.4 \% \) at end isovolumetric relaxation, before returning back to zero at end diastole.

Fig. 4 displays the spatio-temporal evolution of the average cardiac strains across the anterior-basal left ventricular wall over three consecutive beats, where red indicates positive, i.e., tensile strains, and blue indicates negative, i.e., compressive strains. Mechanical activation characterized through the transition from red to blue in the circumferential strain \( E_{CC} \) begins at the endocardium, the inner wall, at
Fig. 3 – Temporal evolution of cardiac strains at 50% depth of the anterior-basal left ventricular wall. Maximum circumferential contraction $E_{CC}$ is $-7.9 \pm 3.8\%$ and maximum wall thickening $E_{RR}$ is $+11.3 \pm 6.4\%$. Means and standard deviations of components of the Green–Lagrange strains are displayed for $n = 9$ animals to the top of the curves. C circumferential, R radial, and L longitudinal direction. ED end diastole, EIR end isovolumetric relaxation, ES end systole, and EIC end isovolumetric contraction.

Fig. 4 – Spatio-temporal evolution of cardiac strains in the anterior-basal left ventricular wall averaged over $n = 9$ animals. Components of the Green–Lagrange strains are displayed across the ventricular wall with 10% depth indicating the epicardium, the outer wall, and 90% depth indicating the endocardium, the inner wall. Strains are displayed for three consecutive heartbeats. C circumferential, R radial, and L longitudinal direction. ED end diastole, EIR end isovolumetric relaxation, ES end systole, and EIC end isovolumetric contraction.

90% depth, and then progresses towards the epicardium, the outer wall, at 10% depth. Mechanical deactivation, however, progresses vice versa, beginning at the epicardium and progressing towards the endocardium. This implies that the cells that are activated first are deactivated last. Mechanical deactivation proceeds faster than mechanical activation as
Fig. 5 – Temporal evolution of cardiac strains at 50% depth of the lateral-equatorial left ventricular wall. Maximum circumferential contraction is $-7.9 \pm 3.8\%$ and maximum wall thickening is $+10.5 \pm 5.2\%$. Means and standard deviations of components of the Green–Lagrange strains are displayed for $n = 9$ animals to the top of the curves. C circumferential, R radial, and L longitudinal direction. ED end diastole, EIR end isovolumetric relaxation, ES end systole, and EIC end isovolumetric contraction.

Fig. 6 – Spatio-temporal evolution of cardiac strains in the lateral-equatorial left ventricular wall averaged over $n = 9$ animals. Components of the Green–Lagrange strains are displayed across the ventricular wall with 10% depth indicating the epicardium, the outer wall, and 90% depth indicating the endocardium, the inner wall. Strains are displayed for three consecutive heartbeats. C circumferential, R radial, and L longitudinal direction. ED end diastole, EIR end isovolumetric relaxation, ES end systole, and EIC end isovolumetric contraction.

indicated by the steeper slope in the transition from blue to red. This mechanical excitation pattern closely resembles the electrical excitation pattern starting at the endocardium, progressing gradually outward towards the epicardium, as
the activation wave spreads across the heart (Durrer et al., 1970). This observation is in excellent agreement with the electrophysiological response of endocardial cells, close to the Purkinje fiber system, which display a longer action potential duration than epicardial cells (Göktepe et al., 2010; Kotikanyadam et al., 2010), meaning they are electrically activated first and deactivated last. Temporal strain variations throughout the cardiac cycle are larger in the endocardium than in the epicardium for both circumferential $E_{CC}$ and radial $E_{RR}$ strains.

4.3. Spatio-temporal evolution of cardiac strains in the lateral wall

Fig. 5 displays the temporal evolution of the average cardiac strains at the lateral-equatorial left ventricular midwall, i.e., at 50% depth. For all six strain components, the general trend in the lateral-equatorial wall is similar to the anterior-basal wall, displayed in Fig. 3. There are some minor differences in the circumferential strains $E_{CC}$ at end isovolumetric relaxation, which seem to be less pronounced in the lateral midwall at $-5.1 \pm 6.0\%$ than in the anterior midwall at $-7.9 \pm 3.8\%$. However, the longitudinal extension $E_{LL}$ at end isovolumetric contraction seems to be more pronounced in the lateral midwall at $+4.9 \pm 4.4\%$ than in the anterior midwall at $+0.8 \pm 3.8\%$.

Fig. 6 depicts the spatio-temporal evolution of the average cardiac strains across the lateral-equatorial left ventricular wall, where, again, red indicates positive, i.e., tensile strains, and blue indicates negative, i.e., compressive strains. The general trend seems to be similar to that of the anterior wall, displayed in Fig. 5. Overall, transmural strain variations in the lateral wall seem to be less pronounced than those in the anterior wall, except for the change in the radial strain which is similar to that of the anterior wall. In addition, mechanical activation of the lateral-equatorial wall seems to be slightly delayed as compared to that of the anterior-basal wall. This manifests itself in both circumferential $E_{CC}$ and radial $E_{RR}$ strains which are mechanically activated only at end systole. This mechanical activation delay agrees nicely with the electrical activation delay of the lateral-equatorial wall with respect to the anterior-basal wall, which has been reported to be one of the regions of early electrical activation (Durrer et al., 1970).

4.4. Spatio-temporal evolution of fiber strains in the anterior and lateral wall

Fig. 7 illustrates the temporal evolution of the average fiber strains $E_{FF}$, both in the anterior-basal and lateral-equatorial left ventricular wall. The general trends are similar in the anterior and lateral wall. Transmurally, the maximum fiber stretch $E_{FF}$ occurs at end isovolumetric contraction at $+3.5 \pm 4.1\%$ close to the epicardium, decreasing transmurally towards the endocardium, where the maximum fiber stretch $E_{FF}$ is less than $+0.5 \pm 0.9\%$. Transmurally, the maximum fiber contraction $E_{FF}$ occurs between end systole and end isovolumetric relaxation at $-8.0 \pm 2.5\%$ close to the endocardium and in the midwall, decreasing transmurally towards the epicardium, where maximum fiber contraction $E_{FF}$ is only $-6.2 \pm 4.6\%$. Overall, this indicates that fiber strains display a significant transmural heterogeneity, being more contractile in the inner wall than in the outer wall and more contractile at the anterior site than at the lateral site. Temporally, maximum fiber contraction is found between end systole and isovolumetric relaxation in the endocardium, progressing across the wall and reaching the epicardium at end isovolumetric relaxation. In this sense, the mechanical activation sequence nicely follows the electrical activation sequence, from endocardium to epicardium, from the anterior-basal to the lateral-equatorial wall, reported in the literature (Durrer et al., 1970). In general, fiber contraction seems to be more pronounced and more coordinated in the anterior-basal than in the lateral-equatorial wall.

Last, Fig. 8 summarizes the spatio-temporal evolution of the average fiber strains $E_{FF}$, both in the anterior-basal and lateral-equatorial wall. It confirms the general trends observed in Fig. 7. Fiber shortening, represented through blue colors, seems to be more coordinated in the anterior than in the lateral wall. Fiber pre-stretch, indicated through red colors, spans the entire anterior-basal wall and the upper half of the lateral-equatorial wall. Some small pre-stretched regions in the endocardium of the lateral-equatorial wall might be attributed to the tension exerted by the papillary muscles located in this area. Fiber strain profiles are transmurally homogeneous at end diastole, see the almost vertical orange zero-strain lines near end diastole in Fig. 8, top and bottom. This indicates that fiber relaxation occurs almost simultaneously across the wall both in the anterior and lateral regions. However, fiber strain profiles are transmurally heterogeneous during systole, see the inclined orange zero-strain lines from end isovolumetric contraction towards end systole in Fig. 8, top and bottom. This indicates that fiber contraction is initiated at the endocardium slightly after end diastole and progresses transmurally outward, reaching the epicardium slightly before end systole. Fiber relaxation, indicated through the transition from blue to orange, proceeds faster than the fiber contraction, indicated through the transition from orange to blue. Accordingly, fibers near the outer wall are in contraction for approximately half of the cardiac cycle while fibers near the inner wall are in contraction almost throughout the entire cardiac cycle. Roughly speaking, in Fig. 8, blue contractile regions with $E_{FF} < 0$ are more pronounced close to the endocardium, while red tensile regions with $E_{FF} > 0$ are more pronounced close to the epicardium. This effect is more pronounced in the anterior-basal than in the lateral-equatorial wall.

5. Discussion

5.1. Limitations

A limitation inherent to the proposed marker technique is that it is invasive in nature and therefore not applicable to humans. Although ovine hearts behave relatively similar to human hearts, we need to be careful when extrapolating our findings to cardiac wall dynamics in humans. In fact, the overall goal of this research is to utilize our videofluoroscopic marker technique to validate common non-invasive imaging
Fig. 7 – Temporal evolution of fiber strains at 20%, 50%, and 80% depth of the anterior-basal and lateral-equatorial left ventricular wall. Maximum fiber contraction varies from \(-8.0 \pm 2.5\%\) and \(-5.4 \pm 3.1\%\) in the anterior and lateral endocardium, i.e., at 80% depth, to \(-6.2 \pm 4.6\%\) and \(-4.6 \pm 4.2\%\) in the anterior and lateral epicardium, i.e., at 20% depth. Means and standard deviations are displayed for \(n = 9\) animals to the top of the curves. ED end diastole, EIR end isovolumetric relaxation, ES end systole, and EIC end isovolumetric contraction.

Fig. 8 – Spatio-temporal evolution of fiber strains in the anterior-basal and lateral-equatorial left ventricular wall averaged over \(n = 9\) animals. Fiber strains are displayed across the ventricular wall with 10% depth indicating the epicardium, the outer wall, and 90% depth indicating the endocardium, the inner wall. Strains are displayed for three consecutive heartbeats. ED end diastole, EIR end isovolumetric relaxation, ES end systole, and EIC end isovolumetric contraction.

Techniques used in human patients in the clinic such as tissue Doppler imaging and speckle tracking echocardiography. Another potential limitation might be that we perform the data acquisition right after the surgical procedure itself. The implantation of myocardial markers and transmural beads is an invasive procedure associated with local left ventricular wall trauma which might potentially lead to acute changes in ventricular wall dynamics. This might explain our relatively low ejection fraction and our relatively low strain values when compared with canine models reported in the literature (Waldman et al., 1985), which, however, agree relatively well with our previous results in ovine models (Cheng et al., 2006a). To quantify these acute effects, we have previously acquired marker and bead coordinates immediately after implantation and several weeks post surgery. While hemodynamics were unfavorably impacted by the surgical intervention, differences in absolute strain values were only minor, and general trends remained unchanged.
Lastly, it could be viewed as a limitation that the results of our computational analysis are sensitive to the chosen reference configuration. After experimenting with different reference configurations, we have chosen end diastole as the strain free reference state. While the choice of the reference state obviously influences the absolute values of the individual strain components, general trends remain unaltered. Different reference configurations basically induce a vertical shift of the strain vs. time curves, but the strain amplitudes remain virtually unchanged. To extract fiber strains, we have used generic fiber orientation maps generated by tissue histology averaged over five animals. It would, of course, be more appropriate to utilize subject-specific fiber orientation maps when projecting the strain tensor onto local fiber directions.

5.2. Clinical significance

Left ventricular wall strains and active fiber contraction are believed to be important indicators for left ventricular remodeling. Altered wall strains can result in the production of cytokines and reactive oxygen species stimulating cardiomyocyte apoptosis and extracellular matrix disruption which, in turn, might trigger global left ventricular dilation and remodeling. This study therefore aimed at establishing a baseline characterization of cardiac and fiber strains throughout the cardiac cycle to quantify temporal, regional, and transmural variations of active fiber contraction in the healthy beating heart. Our observed mechanical excitation patterns are in excellent qualitative agreement with the electrical excitation patterns reported in the literature (Durrer et al., 1970). They complement our in vitro database of strains and stresses in healthy cardiac muscle tissue (Böl et al., in press). The identification of deviations from these baseline values is clinically important to guide the optimal timing of clinical interventions, e.g., in asymptomatic severe mitral regurgitation (Carhäll et al., 2008) or in progressive heart failure (Göktepe et al., 2010). The permanent nature of the implanted beads renders the proposed marker technology an ideal methodology to quantify chronic kinematic changes during progressive growth and remodeling (Göktepe et al., 2010).

5.3. Engineering relevance

The past two decades have seen a clear trend towards patient-specific computational treatment planning in cardiovascular disease. This manuscript has established a baseline characterization of ventricular wall dynamics that might be useful to calibrate and validate mechanistic material models and computational simulation tools for passive cardiac relaxation (Göktepe et al., 2011), active cardiac contraction (Göktepe and Kuhl, 2010), and potential viscous effects (Katsnelson et al., 2004). Lastly, and maybe most importantly, current therapies for heart failure seek to support the ventricular wall to reduce cardiomyocyte overstretch by using synthetic or living tissue engineered solutions (Christman and Lee, 2006). This study provides useful guidelines for the structural and functional requirements of these biomaterials and may therefore be relevant to tissue engineering in general.

6. Conclusions

In summary, this study demonstrates that cardiac wall strains display significant temporal, regional, and transmural variations. Maximum fiber contraction was found to vary from $-8.0 \pm 2.5\%$ and $-5.4 \pm 3.1\%$ in the anterior and lateral endocardium to $-6.2 \pm 4.6\%$ and $-4.6 \pm 4.2\%$ in the anterior and lateral epicardium. Mechanical activation is initiated at the endocardium progressing transmurally outwards towards the epicardium, whereas mechanical deactivation occurs almost simultaneously across the wall. Fibers near the outer wall are therefore in contraction for approximately half of the cardiac cycle while fibers near the inner wall are in contraction almost throughout the entire cardiac cycle. We believe that this work provides a valuable baseline data set to judge strain alterations in response to cardiac disease and treatment, to validate alternative non-invasive imaging modalities, to calibrate and validate material models and computational tools for active cardiac contraction, and to engineer synthetic or living biomaterials with similar structure and function.

Acknowledgments

This work was supported by the US National Institutes of Health grants R01 HL 29589 and R01 HL67025 (Dr. Miller); the US National Science Foundation CAREER award CMMI-0952921 (Dr. Kuhl); the Swiss National Science Foundation Fellowship PBELP2-130913 (Dr. Tsamis); the Western States Affiliate American Heart Association Fellowship (Dr. Swan- son); the US–Norway Fulbright Foundation, the Swedish Heart–Lung Foundation, and the Swedish Society for Medical Research (Dr. Kvitting); and the Deutsche Herzstiftung, Frankfurt, Germany, Research Grant S/06/07 (Dr. Bothe).

References


